

## الباب الثالث عشر

### امتحانات متنوعة

#### Various Exams

جامعة قناة السويس	الفرقة: إعدادي
كلية هندسة البترول والتعدين بالسويس	الزمن : ساعة و نصف
قسم العلوم والرياضيات الهندسية	التاريخ: 17/1/2010
تخلفات تفاضل	
امتحان نهاية التيرم الأول	

أجب عن الأسئلة الآتية:

السؤال الأول: ( 25 درجة)

(ا) عرف كل من الدوال الآتية موضحا بالرسم: دالة الجيب- دالة جيب التمام.

(ب) باستخدام التعريف العام للتفاضل أوجد المشتقة الأولى للدالة الآتية :  $y = \cos x$

(ج) أوجد المعامل التفاضلي للدوال الآتية:  $y = \operatorname{cosec} x$

$y = \cosh x$

(د) اوجد المشتقة النونية للدالة الآتية:  $y = x^4 e^{-3x}$

السؤال الثاني: ( 25 درجة)

(أ) إذا كانت  $f(x) \in N(4,3), f(x) = 3x + 7$  أوجد  $\varepsilon$  لكل

$$x \in N(-1, 0.1)$$

$$\lim_{x \rightarrow 2} \frac{3x + 4}{5x + 7}$$

(ب) اوجد نهاية الدالة

$$f(x) = \begin{cases} 3x - 2 & \text{if } x < 2 \\ x^2 & \text{if } x > 2 \end{cases}$$

(ج) اذا كانت

$$\lim_{x \rightarrow 2} f(x)$$

اوجد

(د) هل تحقق الدالة  $y = x^2 |x|$  شروط نظرية رول في الفترة

$$[-1, 1]$$

السؤال الثالث: (25 درجة)

(أ) باستخدام قاعدة اوبيتال احسب النهايات التالية :  $\lim_{x \rightarrow 2} \frac{\ln(x^2 - 3)}{x^2 + 3x - 10}$

(ب) اوجد متسلسلة مكلورين للدالة  $\cos x$  والدالة  $\ln(1 + x)$

في قوى  $x$  التصاعديّة .

$$f(x) = (x + 5)^2 \sqrt[3]{x-4}$$

(ج) اوجد النقطة الحرجة للدالة

(د) : اوجد معادلتى المماس والعمودى للمنحنى

$$\sqrt{x/y} + \sqrt{y/x} = 5/2 \text{ عند النقطة } (6, 3) .$$

ا. د/ عادل نسيم

مع تمنياتي بالنجاح

الفرقة: إعدادي  
الزمن: ساعة و نصف  
التاريخ: 2009/1/22

جامعة قناة السويس  
كلية هندسة البترول والتعدين بالسويس  
قسم العلوم والرياضيات الهندسية  
تفاضل

امتحان نهاية التيرم الأول 2009/2008

أجب عن الأسئلة الآتية:

السؤال الأول: (17 درجة)

(أ) عرف كل من موضعا بالرسم: دالة الجيب- دالة جيب التمام.  
(ب) باستخدام التعريف العام للتفاضل أوجد المشتقة الأولى للدالة الآتية

$$y = \ln x :$$

(ج) أوجد المعامل التفاضلي للدوال الآتية:

$$y = \cosh x \text{ و } y = \tan x$$

(د) أوجد المشتقة النونية للدالة الآتية:

$$y = x^4 e^{-3x}$$

السؤال الثاني: (17 درجة)

(أ) إذا كانت  $f(x) = 3x + 7$ ,  $f(x) \in N(4,3)$  أوجد  $\varepsilon$  لكل  $x \in N(-1,0.1)$

$$\lim_{x \rightarrow 2} \frac{3x+4}{5x+7}$$

(ب) أوجد نهاية الدالة

$$f(x) = \begin{cases} 3x-2 & \text{if } x < 2 \\ x^2 & \text{if } x > 2 \end{cases}$$

(ج) إذا كانت

$$\lim_{x \rightarrow 2} f(x) \text{ أوجد}$$

(د) هل تحقق الدالة  $y = x^2 |x|$  شروط نظرية رول في الفترة

$[-1, 1]$ .

السؤال الثالث: (16 درجة)

أ) باستخدام قاعدة اوبيتال احسب النهايات التالية :  $\lim_{x \rightarrow 2} \frac{\ln(x^2 - 3)}{x^2 + 3x - 10}$

ب) اوجد متسلسلة مكلورين للدالة  $\cos x$  والدالة  $\ln(1 - x)$  في قوى  $x$  التصاعديّة .

ج) اوجد النقطة الحرجة للدالة  $f(x) = (x + 5)^2 \sqrt[3]{x-4}$

د) : أوجد معادلتى المماس والعمودى للمنحنى  $\sqrt{x/y} + \sqrt{y/x} = 5/2$  عند النقطة  $(6, 3)$  .

مع تمنياتي بالنجاح ا. د/ عادل نسيم

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